

Rational functions:  $f(x) = \frac{p(x)}{q(x)}$  . Restriction:  $q(x) \neq 0$

Base Functions:	$f(x) = \frac{1}{x}$	$f(x) = \frac{1}{x^2}$
Transformations:	$g(x) = \frac{a}{b(x-h)} + k$	$g(x) = \frac{a}{(b(x-h))^2} + k$
Vertical asymptotes:	$x = h$	$x = h$
Horizontal asymptotes:	$y = k$	$y = k$
Vertical stretch:	a	a
Mapping Notation:	$\left(\frac{1}{b}x + h, ay + k\right)$	$\left(\frac{1}{b}x + h, ay + k\right)$

Domain – possible values for  $x$

Range – possible values for  $y$

### Graphing Rational Functions/Writing Equations of Rational Functions

- ***x-intercept:*** a factor of ***only*** the numerator
- ***vertical asymptote:*** a factor of ***only*** the denominator
- ***point of discontinuity:*** a factor of ***both*** the numerator and the denominator
- find  $y$ -intercept (let  $x = 0$ )
- sign analysis: tells where the graph is positive and negative
- horizontal asymptote:
  - a) if numerator degree = denominator degree,  $y =$  ratio of leading coefficients
  - b) If numerator degree < denominator degree,  $y = 0$

Solving Rational Equations Algebraically – watch for extraneous roots!

**Review Questions:** Page 468 #1 – 3, 5, 6, 8a, 9 (alg. only), 10a (alg. only)

Page 470 #1, 2, 6, 7 (alg. only), 8, 10, 11, 12