

$y = f(x) + k$ if $k > 0$, a vertical translation of “ k ” units **up**
 if $k < 0$, a vertical translation of “ k ” units **down**

$y = f(x - h)$ if $h > 0$, a horizontal translation of “ h ” units **to the right**.
 if $h < 0$, a horizontal translation of “ h ” units **to the left**.

$y = -f(x)$ a reflection in the x-axis

$y = f(-x)$ a reflection in the y-axis

$y = af(x)$ a vertical stretch about the x-axis by a factor of $|a|$

$y = f(bx)$ a horizontal stretch about the y-axis by a factor of $\frac{1}{|b|}$

$y = af(b(x - h)) + k$

Mapping Notation (image points): $(x, y) \rightarrow \left(\frac{1}{b}x + h, ay + k \right)$

Invariant points – points that remain the same after a transformation is applied.

Writing equations: Look at stretches (a and b) and reflections ($-a$ and $-b$) first. Then look at translations/shifts (h and k).

Inverse of a relation:

- interchange the x-coordinates and y-coordinates
- the graph of the inverse is a reflection of the relation in the line $y = x$
- domain and range are reversed
- if the inverse of a function $f(x)$ is a function, it is written $f^{-1}(x)$

Review Questions